

## **pst-3d** **basic three dimension functions** v.1.10

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This version of `pst-3d` uses the extended keyval handling of `pst-xkey`.

Thanks to:

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## 1 PostScript functions SetMatrixThreeD, ProjThreeD, and SetMatrixEmbed

The viewpoint for 3D coordinates is given by three angles:  $\alpha$ ,  $\beta$  and  $\gamma$ .  $\alpha$  and  $\beta$  determine the direction from which one is looking.  $\gamma$  then determines the orientation of the observing.

When  $\alpha$ ,  $\beta$  and  $\gamma$  are all zero, the observer is looking from the negative part of the  $y$ -axis, and sees the  $xz$ -plane the way in 2D one sees the  $xy$  plan. Hence, to convert the 3D coordinates to their 2D project,  $\langle x, y, z \rangle$  map to  $\langle x, z \rangle$ .

When the orientation is different, we rotate the coordinates, and then perform the same projection.

We move up to latitude  $\beta$ , over to longitude  $\alpha$ , and then rotate by  $\gamma$ . This means that we first rotate around  $y$ -axis by  $\gamma$ , then around  $x$ -axis by  $\beta$ , and the around  $z$ -axis by  $\alpha$ .

Here are the matrices:

$$\begin{aligned} R_z(\alpha) &= \begin{bmatrix} \cos \alpha & -\sin \alpha & 0 \\ \sin \alpha & \cos \alpha & 0 \\ 0 & 0 & 1 \end{bmatrix} \\ R_x(\beta) &= \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \beta & \sin \beta \\ 0 & -\sin \beta & \cos \beta \end{bmatrix} \\ R_y(\gamma) &= \begin{bmatrix} \cos \gamma & 0 & -\sin \gamma \\ 0 & 1 & 0 \\ \sin \gamma & 0 & \cos \gamma \end{bmatrix} \end{aligned}$$

The rotation of a coordinate is then performed by the matrix  $R_z(\alpha)R_x(\beta)R_y(\gamma)$ . The first and third columns of the matrix are the basis vectors of the plan upon which the 3D coordinates are project (the old basis vectors were  $\langle 1, 0, 0 \rangle$  and  $\langle 0, 0, 1 \rangle$ ; rotating these gives the first and third columns of the matrix).

These new basis vectors are:

$$\begin{aligned} \tilde{x} &= \begin{bmatrix} \cos \alpha \cos \gamma - \sin \beta \sin \alpha \sin \gamma \\ \sin \alpha \cos \gamma + \sin \beta \cos \alpha \sin \gamma \\ \cos \beta \sin \gamma \end{bmatrix} \\ \tilde{z} &= \begin{bmatrix} -\cos \alpha \sin \gamma - \sin \beta \sin \alpha \cos \gamma \\ -\sin \alpha \sin \gamma + \sin \beta \cos \alpha \cos \gamma \\ \cos \beta \cos \gamma \end{bmatrix} \end{aligned}$$

Rather than specifying the angles  $\alpha$  and  $\beta$ , the user gives a vector indicating where the viewpoint is. This new viewpoint is the rotation of the old viewpoint. The old viewpoint is  $\langle 0, -1, 0 \rangle$ , and so the new viewpoint is

$$R_z(\alpha)R_x(\beta) \begin{bmatrix} 0 \\ -1 \\ 0 \end{bmatrix} = \begin{bmatrix} \cos \beta \sin \alpha \\ -\cos \beta \cos \alpha \\ \sin \beta \end{bmatrix} = \begin{bmatrix} v_1 \\ v_2 \\ v_3 \end{bmatrix}$$

Therefore,

$$\begin{aligned}\alpha &= \arctan(v_1 / -v_2) \\ \beta &= \arctan(v_3 \sin \alpha / v_1)\end{aligned}$$

Unless  $p_1 = p_2 = 0$ , in which case  $\alpha = 0$  and  $\beta = \text{sign}(p_3)90$ , or  $p_1 = p_3 = 0$ , in which case  $\beta = 0$ .

The syntax of `SetMatrixThreeD` is  $v_1 \ v_2 \ v_3 \ \gamma \ \text{SetMatrixThreeD}$   
`SetMatrixThreeD` first computes

$$\begin{aligned}a &= \sin \alpha & b &= \cos \alpha \\ c &= \sin \beta & d &= \cos \beta \\ e &= \sin \gamma & f &= \cos \gamma\end{aligned}$$

and then sets `Matrix3D` to  $[\tilde{x} \ \tilde{z}]$ .

```

1 /SetMatrixThreeD {
2   dup sin /e ED cos /f ED
3   /p3 ED /p2 ED /p1 ED
4   p1 0 eq
5   { /a 0 def /b p2 0 le { 1 } { -1 } ifelse def
6     p3 p2 abs
7   }
8   { p2 0 eq
9     { /a p1 0 lt { -1 } { 1 } ifelse def /b 0 def
10      p3 p1 abs
11    }
12    { p1 dup mul p2 dup mul add sqrt dup
13      p1 exch div /a ED
14      p2 exch div neg /b ED
15      p3 p1 a div
16    }
17    ifelse
18  }
19  ifelse
20  atan dup sin /c ED cos /d ED
21  /Matrix3D
22  [
23    b f mul c a mul e mul sub
24    a f mul c b mul e mul add
25    d e mul
26    b e mul neg c a mul f mul sub
27    a e mul neg c b mul f mul add
28    d f mul
29  ] def
30 } def

```

The syntax of `ProjThreeD` is  $x \ y \ z \ \text{ProjThreeD} \ x' \ y'$  where  $x' = \langle x, y, z \rangle \cdot \tilde{x}$  and  $y' = \langle x, y, z \rangle \cdot \tilde{z}$ .

```

1 /ProjThreeD {
2   /z ED /y ED /x ED

```

```

3 Matrix3D aload pop
4 z mul exch y mul add exch x mul add
5 4 1 roll
6 z mul exch y mul add exch x mul add
7 exch
8 } def

```

To embed 2D  $\langle x, y \rangle$  coordinates in 3D, the user specifies the normal vector and an angle. If we decompose this normal vector into an angle, as when converting 3D coordinates to 2D coordinates, and let  $\hat{\alpha}$ ,  $\hat{\beta}$  and  $\hat{\gamma}$  be the three angles, then when these angles are all zero the coordinate  $\langle x, y \rangle$  gets mapped to  $\langle x, 0, y \rangle$ , and otherwise  $\langle x, y \rangle$  gets mapped to

$$R_z(\hat{\alpha})R_x(\hat{\beta})R_y(\hat{\gamma}) \begin{bmatrix} x \\ 0 \\ y \end{bmatrix} = \begin{bmatrix} \hat{x}_1x + \hat{z}_1y \\ \hat{x}_2x + \hat{z}_2y \\ \hat{x}_3x + \hat{z}_3y \end{bmatrix}$$

where  $\hat{x}$  and  $\hat{z}$  are the first and third columns of  $R_z(\hat{\alpha})R_x(\hat{\beta})R_y(\hat{\gamma})$ .

Now add on a 3D-origin:

$$\begin{bmatrix} \hat{x}_1x + \hat{z}_1y + x_0 \\ \hat{x}_2x + \hat{z}_2y + y_0 \\ \hat{x}_3x + \hat{z}_3y + z_0 \end{bmatrix}$$

Now when we project back onto 2D coordinates, we get

$$\begin{aligned} x' &= \tilde{x}_1(\hat{x}_1x + \hat{z}_1y + x_0) + \tilde{x}_2(\hat{x}_2x + \hat{z}_2y + y_0) + \tilde{x}_3(\hat{x}_3x + \hat{z}_3y + z_0) \\ &= (\tilde{x}_1\hat{x}_1 + \tilde{x}_2\hat{x}_2 + \tilde{x}_3\hat{x}_3)x \\ &\quad + (\tilde{x}_1\hat{z}_1 + \tilde{x}_2\hat{z}_2 + \tilde{x}_3\hat{z}_3)y \\ + \tilde{x}_1x_0 + \tilde{x}_2y_0 + \tilde{x}_3z_0 &= \tilde{z}_1(\hat{x}_1x + \hat{z}_1y + x_0) + \tilde{z}_2(\hat{x}_2x + \hat{z}_2y + y_0) + \tilde{z}_3(\hat{x}_3x + \hat{z}_3y + z_0) \\ &= (\tilde{z}_1\hat{x}_1 + \tilde{z}_2\hat{x}_2 + \tilde{z}_3\hat{x}_3)x \\ &\quad + (\tilde{z}_1\hat{z}_1 + \tilde{z}_2\hat{z}_2 + \tilde{z}_3\hat{z}_3)y \\ &\quad + \tilde{z}_1x_0 + \tilde{z}_2y_0 + \tilde{z}_3z_0 \end{aligned}$$

Hence, the transformation matrix is:

$$\begin{bmatrix} \tilde{x}_1\hat{x}_1 + \tilde{x}_2\hat{x}_2 + \tilde{x}_3\hat{x}_3 \\ \tilde{z}_1\hat{x}_1 + \tilde{z}_2\hat{x}_2 + \tilde{z}_3\hat{x}_3 \\ \tilde{x}_1\hat{z}_1 + \tilde{x}_2\hat{z}_2 + \tilde{x}_3\hat{z}_3 \\ \tilde{z}_1\hat{z}_1 + \tilde{z}_2\hat{z}_2 + \tilde{z}_3\hat{z}_3 \\ \tilde{x}_1x_0 + \tilde{x}_2y_0 + \tilde{x}_3z_0 \\ \tilde{z}_1x_0 + \tilde{z}_2y_0 + \tilde{z}_3z_0 \end{bmatrix}$$

The syntax of `SetMatrixEmbed` is  $x_0 \ y_0 \ z_0 \ \hat{v}_1 \ \hat{v}_2 \ \hat{v}_3 \ \hat{\gamma} \ v_1 \ v_2 \ v_3 \ \gamma$  `SetMatrixEmbed`

`SetMatrixEmbed` first sets  $\langle x_1 \ x_2 \ x_3 \ y_1 \ y_2 \ y_3 \rangle$  to the basis vectors for the view-point projection (the tilde stuff above). Then it sets `Matrix3D` to the basis vectors for the embedded plane. Finally, it sets the transformation matrix to the matrix given above.

```

1 /SetMatrixEmbed {

```

```

2 SetMatrixThreeD
3 Matrix3D aload pop
4 /z3 ED /z2 ED /z1 ED /x3 ED /x2 ED /x1 ED
5 SetMatrixThreeD
6 [
7 Matrix3D aload pop
8 z3 mul exch z2 mul add exch z1 mul add 4 1 roll
9 z3 mul exch z2 mul add exch z1 mul add
10 Matrix3D aload pop
11 x3 mul exch x2 mul add exch x1 mul add 4 1 roll
12 x3 mul exch x2 mul add exch x1 mul add
13 3 -1 roll 3 -1 roll 4 -1 roll 8 -3 roll 3 copy
14 x3 mul exch x2 mul add exch x1 mul add 4 1 roll
15 z3 mul exch z2 mul add exch z1 mul add
16 ]
17 concat
18 } def

```

## 2 Keywords

### 2.1 viewpoint

```

1 \let\pssetzlength\pssetylength
2 \define@key[psset]{pst-3d}{viewpoint}{%
3 \pst@expandafter\psset@@viewpoint#1 {} {} {} \@nil
4 \let\psk@viewpoint\pst@tempg}
5 \def\psset@@viewpoint#1 #2 #3 #4\@nil{%
6 \begingroup
7 \pssetxlength\pst@dima{#1}%
8 \pssetylength\pst@dimb{#2}%
9 \pssetzlength\pst@dimc{#3}%
10 \xdef\pst@tempg{%
11 \pst@number\pst@dima \pst@number\pst@dimb \pst@number\pst@dimc}%
12 \endgroup}
13 \psset[pst-3d]{viewpoint=1 -1 1}

```

### 2.2 viewangle

```

1 \define@key[psset]{pst-3d}{viewangle}{\pst@getangle{#1}\psk@viewangle}
2 \psset[pst-3d]{viewangle=0}

```

### 2.3 normal

```

1 \define@key[psset]{pst-3d}{normal}{%
2 \pst@expandafter\psset@@viewpoint#1 {} {} {} \@nil
3 \let\psk@normal\pst@tempg}
4 \psset[pst-3d]{normal=0 0 1}

```

## 2.4 embedangle

```
1 \define@key[psset]{pst-3d}{embedangle}{\pst@getangle{#1}\psk@embedangle}
2 \psset[pst-3d]{embedangle=0}
```

## 3 Transformation matrix

```
1 /TMSave {
2   tx@Dict /TMatrix known not { /TMatrix { } def /RAngle { 0 } def } if end
3   /TMatrix [ TMatrix CM ] cvx def
4 } def
5 /TMRestore { CP /TMatrix [ TMatrix setmatrix ] cvx def moveto } def
6 /TMChange {
7   TMSave
8   /cp [ currentpoint ] cvx def % Check this later.CM def
```

Set standard coord. system, with pt units and origin at currentpoint. This lets us rotate, or whatever, around  $\text{T}_{\text{E}}\text{X}$ 's current point, without having to worry about strange coordinate systems that the dvi-to-ps driver might be using.

```
1 CP T STV
```

Let  $M$  = old matrix (on stack), and  $M'$  equal current matrix. Then go from  $M'$  to  $M$  by applying  $M \text{ Inv}(M')$ .

```
1 CM matrix invertmatrix % Inv(M')
2 matrix concatmatrix % M Inv(M')
```

Now modify transformation matrix:

```
1 exch exec
```

Now apply  $M \text{ Inv}(M')$

```
1 concat cp moveto
```

## 4 Macros

### 4.1 \ThreeDput

```
1 \def\ThreeDput{\pst@object{ThreeDput}}
2 \def\ThreeDput@i{\@ifnextchar({\ThreeDput@ii}{\ThreeDput@ii(\z@,\z@,\z@)}}
3 \def\ThreeDput@ii(#1,#2,#3){%
4   \pst@killglue\pst@makebox{\ThreeDput@iii(#1,#2,#3)}}
5 \def\ThreeDput@iii(#1,#2,#3){%
6   \begingroup
7   \use@par
8   \if@star\pst@starbox\fi
9   \pst@makesmall\pst@hbox
```



```

10 \pssetxlength\pst@dim{#1}%
11 \pssetylength\pst@dim{#2}%
12 \pssetzlength\pst@dim{#3}%
13 \leavevmode
14 \hbox{%
15   \pst@Verb{%
16     { \pst@number\pst@dim{
17       \pst@number\pst@dim{
18       \pst@number\pst@dim{
19       \psk@normal
20       \psk@embedangle
21       \psk@viewpoint
22       \psk@viewangle
23       \tx@SetMatrixEmbed
24     } \tx@TMChange}%
25   \box\pst@hbox
26   \pst@Verb{\tx@TMRestore}}}%
27 \endgroup
28 \ignorespaces}

```

## 5 Arithmetic

`\pst@divide` This is adapted from Donald Arseneau's `shapepar.sty`. Syntax:

```

\pst@divide{<numerator>}{<denominator>}{<command>}
\pst@@divide{<numerator>}{<denominator>}

```

`<numerator>` and `<denominator>` should be dimensions. `\pst@divide` sets `<command>` to `<num>/<den>` (in points). `\pst@@divide` sets `\pst@dim` to `<num>/<den>`.

```

1 \def\pst@divide#1#2#3{%
2   \pst@@divide{#1}{#2}%
3   \pst@dimtonum\pst@dim{#3}}
4 \def\pst@@divide#1#2{%
5   \pst@dim=#1\relax
6   \pst@dimh=#2\relax
7   \pst@cntg=\pst@dimh
8   \pst@cnth=67108863
9   \pst@@@divide\pst@@@divide\pst@@@divide\pst@@@divide
10  \divide\pst@dim\pst@cntg}

```

The number 16 is the level of uncertainty. Use a lower power of 2 for more accuracy (2 is most precise). But if you change it, you must change the repetitions of `\pst@@@divide` in `\pst@@divide` above:

$$\text{precision}^{\text{repetitions}} = 65536$$

(E.g.,  $16^4 = 65536$ ).

```

1 \def\pst@@@divide{%
2   \ifnum

```

```

3 \ifnum\pst@dimg<\z@-\fi\pst@dimg<\pst@cntn
4 \multiply\pst@dimg\sixt@@n
5 \else
6 \divide\pst@cntg\sixt@@n
7 \fi}

```

\pst@pyth Syntax:

\pst@pyth{<dim1>}{<dim2>}{<dimen register>}

<dimen register> is set to  $((dim1)^2 + (dim2)^2)^{1/2}$ .

The algorithm is copied from PiCTeX, by Michael Wichura (with permission). Here is his description:

Suppose  $x > 0$ ,  $y > 0$ . Put  $s = x + y$ . Let  $z = (x^2 + y^2)^{1/2}$ . Then  $z = s \times f$ , where

$$f = (t^2 + (1 - t)^2)^{1/2} = ((1 + \tau^2)/2)^{1/2}$$

and  $t = x/s$  and  $\tau = 2(t - 1/2)$ .

```

1 \def\pst@pyth#1#2#3{%
2 \begingroup
3 \pst@dima=#1\relax
4 \ifnum\pst@dima<\z@\pst@dima=-\pst@dima\fi % dima=abs(x)
5 \pst@dimb=#2\relax
6 \ifnum\pst@dimb<\z@\pst@dimb=-\pst@dimb\fi % dimb=abs(y)
7 \advance\pst@dimb\pst@dima % dimb=s=abs(x)+abs(y)
8 \ifnum\pst@dimb=\z@
9 \global\pst@dimg=\z@ % dimg=z=sqrt(x^2+y^2)
10 \else
11 \multiply\pst@dima 8\relax % dima= 8abs(x)
12 \pst@@divide\pst@dima\pst@dimb % dimg =8t=8abs(x)/s
13 \advance\pst@dimg -4pt % dimg = 4tau = (8t-4)
14 \multiply\pst@dimg 2
15 \pst@dimtonum\pst@dimg\pst@tempa
16 \pst@dima=\pst@tempa\pst@dimg % dima=(8tau)^2
17 \advance\pst@dima 64pt % dima=u=[64+(8tau)^2]/2
18 \divide\pst@dima 2\relax % =(8f)^2
19 \pst@dimd=7pt % initial guess at sqrt(u)
20 \pst@@pyth\pst@@pyth\pst@@pyth % dimd=sqrt(u)
21 \pst@dimtonum\pst@dimd\pst@tempa
22 \pst@dimg=\pst@tempa\pst@dimb
23 \global\divide\pst@dimg 8 % dimg=z=(8f)*s/8
24 \fi
25 \endgroup
26 #3=\pst@dimg}
27 \def\pst@@pyth{% % dimd = g <-- (g + u/g)/2
28 \pst@@divide\pst@dima\pst@dimd
29 \advance\pst@dimd\pst@dimg
30 \divide\pst@dimd 2\relax}

```

\pst@sinandcos Syntax:

\pst@sinandcos{<dim>}{<int>}

<dim>, in sp units, should equal 100,000 times the angle, in degrees between 0 and 90. <int> should equal the angle's quadrant (0, 1, 2 or 3). \pst@dimg is set to  $\sin(\theta)$  and \pst@dimh is set to  $\cos(\theta)$  (in pt's).

The algorithms uses the usual McLaurin expansion.

```

1 \def\pst@sinandcos#1{%
2   \begingroup
3     \pst@dima=#1\relax
4     \pst@dima=.366022\pst@dima %Now 1pt=1/32rad
5     \pst@dimb=\pst@dima % dimb->32sin(angle) in pts
6     \pst@dimc=32\p@ % dimc->32cos(angle) in pts
7     \pst@dimtonum\pst@dima\pst@tempa
8     \pst@cntb=\tw@
9     \pst@cntc=-\@ne
10    \pst@cntg=32
11    \loop
12    \ifnum\pst@dima>\ccclvi % 256
13      \pst@dima=\pst@tempa\pst@dima
14      \divide\pst@dima\pst@cntg
15      \divide\pst@dima\pst@cntb
16      \ifodd\pst@cntb
17        \advance\pst@dimb \pst@cntc\pst@dima
18        \pst@cntc=-\pst@cntc
19      \else
20        \advance\pst@dimc by \pst@cntc\pst@dima
21      \fi
22      \advance\pst@cntb\@ne
23    \repeat
24    \divide\pst@dimb\pst@cntg
25    \divide\pst@dimc\pst@cntg
26    \global\pst@dimg\pst@dimb
27    \global\pst@dimh\pst@dimc
28  \endgroup}

```

\pst@getsinandcos \pst@getsinandcos normalizes the angle to be in the first quadrant, sets \pst@quadrant to 0 for the first quadrant, 1 for the second, 2 for the third, and 3 for the fourth, invokes \pst@sinandcos, and sets \pst@sin to the sine and \pst@cos to the cosine.

```

1 \def\pst@getsinandcos#1{%
2   \pst@dimg=100000sp
3   \pst@dimg=#1\pst@dimg
4   \pst@dimh=36000000sp
5   \pst@cntg=0
6   \loop
7   \ifnum\pst@dimg<\z@
8     \advance\pst@dimg\pst@dimh

```

```

9 \repeat
10 \loop
11 \ifnum\pst@dimg>\pst@dimh
12 \advance\pst@dimg-\pst@dimh
13 \repeat
14 \pst@dimh=9000000sp
15 \def\pst@tempg{%
16 \ifnum\pst@dimg<\pst@dimh\else
17 \advance\pst@dimg-\pst@dimh
18 \advance\pst@cntg\@ne
19 \ifnum\pst@cntg>\thr@@ \advance\pst@cntg-4 \fi
20 \expandafter\pst@tempg
21 \fi}%
22 \pst@tempg
23 \chardef\pst@quadrant\pst@cntg
24 \ifdim\pst@dimg=\z@
25 \def\pst@sin{0}%
26 \def\pst@cos{1}%
27 \else
28 \pst@sinandcos\pst@dimg
29 \pst@dimtonum\pst@dimg\pst@sin
30 \pst@dimtonum\pst@dimh\pst@cos
31 \fi}

```

## 6 Tilting

\pstilt

```

1 \def\pstilt#1{\pst@makebox{\pstilt@{#1}}}
2 \def\pstilt@#1{%
3 \begingroup
4 \leavevmode
5 \pst@getsinandcos{#1}%
6 \hbox{%
7 \ifcase\pst@quadrant
8 \kern\pst@cos\dp\pst@hbox
9 \pst@dima=\pst@cos\ht\pst@hbox
10 \ht\pst@hbox=\pst@sin\ht\pst@hbox
11 \dp\pst@hbox=\pst@sin\dp\pst@hbox
12 \or
13 \kern\pst@sin\ht\pst@hbox
14 \pst@dima=\pst@sin\dp\pst@hbox
15 \ht\pst@hbox=\pst@cos\ht\pst@hbox
16 \dp\pst@hbox=\pst@cos\dp\pst@hbox
17 \or
18 \kern\pst@cos\ht\pst@hbox
19 \pst@dima=\pst@sin\dp\pst@hbox
20 \pst@dimg=\pst@sin\ht\pst@hbox
21 \ht\pst@hbox=\pst@sin\dp\pst@hbox
22 \dp\pst@hbox=\pst@dimg

```

```

23 \or
24 \kern\pst@sin\dp\pst@hbox
25 \pst@dima=\pst@sin\ht\pst@hbox
26 \pst@dimg=\pst@cos\ht\pst@hbox
27 \ht\pst@hbox=\pst@cos\dp\pst@hbox
28 \dp\pst@hbox=\pst@dimg
29 \fi
30 \pst@Verb{%
31 { [ 1 0
32 \pst@cos\space \ifnum\pst@quadrant>\@ne neg \fi
33 \pst@sin\space
34 \ifnum\pst@quadrant>\z@\ifnum\pst@quadrant<\thr@@ neg \fi\fi
35 \ifodd\pst@quadrant exch \fi
36 0 0
37 ] concat
38 } \tx@TMChange}%
39 \box\pst@hbox
40 \pst@Verb{\tx@TMRestore}%
41 \kern\pst@dima}%
42 \endgroup}

```

### \psTilt

```

1 \def\psTilt#1{\pst@makebox{\psTilt@{#1}}}
2 \def\psTilt@#1{%
3 \begingroup
4 \leavevmode
5 \pst@getsinandcos{#1}%
6 \hbox{%
7 \ifodd\pst@quadrant
8 \pst@@divide{\dp\pst@hbox}{\pst@cos\p@}%
9 \ifnum\pst@quadrant=\thr@@\kern\else\pst@dima=\fi\pst@sin\pst@dimg
10 \pst@@divide{\ht\pst@hbox}{\pst@cos\p@}%
11 \ifnum\pst@quadrant=\@ne\kern\else\pst@dima=\fi\pst@sin\pst@dimg
12 \else
13 \ifdim\pst@sin\p@=\z@
14 \@pstrickserr{\string\psTilt\space angle cannot be 0 or 180}\@ehpa
15 \def\pst@sin{.7071}%
16 \def\pst@cos{.7071}%
17 \fi
18 \pst@@divide{\dp\pst@hbox}{\pst@sin\p@}%
19 \ifnum\pst@quadrant=\z@\kern\else\pst@dima=\fi\pst@cos\pst@dimg
20 \pst@@divide{\ht\pst@hbox}{\pst@sin\p@}%
21 \ifnum\pst@quadrant=\tw@\kern\else\pst@dima=\fi\pst@cos\pst@dimg
22 \fi
23 \ifnum\pst@quadrant>\@ne
24 \pst@dimg=\ht\pst@hbox
25 \ht\pst@hbox=\dp\pst@hbox
26 \dp\pst@hbox=\pst@dimg
27 \fi
28 \pst@Verb{%
29 { [ 1 0

```

```

30      \pst@cos\space \pst@sin\space
31      \ifodd\pst@quadrant exch \fi
32      \tx@Div
33      \ifnum\pst@quadrant>\z@\ifnum\pst@quadrant<\thr@@ neg \fi\fi
34      \ifnum\pst@quadrant>\@ne -1 \else 1 \fi
35      0 0
36      ] concat
37      } \tx@TMChange}%
38      \box\pst@hbox
39      \pst@Verb{\tx@TMRestore}%
40      \kern\pst@dim}%
41      \endgroup}

```

\psset@Tshadowsize,\psTshadowsize

```

1 \define@key[psset]{pst-3d}{Tshadowsize}{%
2   \pst@checknum{#1}\psTshadowsize}
3 \psset[pst-3d]{Tshadowsize=1}

```

\psset@Tshadowangle,\psk@Tshadowangle

```

1 \define@key[psset]{pst-3d}{Tshadowangle}{%
2   \pst@getangle{#1}\psk@Tshadowangle}
3 \psset[pst-3d]{Tshadowangle=60}

```

\psset@Tshadowcolor,\psTshadowcolor

```

1 \define@key[psset]{pst-3d}{Tshadowcolor}{%
2   \pst@getcolor{#1}\psTshadowcolor}
3 \psset[pst-3d]{Tshadowcolor=lightgray}

```

\psshadow

```

1 \def\psshadow{\def\pst@par{}\pst@object{psshadow}}
2 \def\psshadow@i{\pst@makebox{\psshadow@ii}}
3 \def\psshadow@ii{%
4   \begingroup
5   \use@par
6   \leavevmode
7   \pst@getsinandcos{\psk@Tshadowangle}%
8   \hbox{%
9     \lower\dp\pst@hbox\hbox{%
10      \pst@Verb{%
11        { [ 1 0
12          \pst@cos\space \psTshadowsize mul
13          \ifnum\pst@quadrant>\@ne neg \fi
14          \pst@sin\space \psTshadowsize mul
15          \ifnum\pst@quadrant>\z@\ifnum\pst@quadrant<\thr@@ neg \fi\fi
16          \ifodd\pst@quadrant exch \fi
17          0 0
18        ] concat
19        } \tx@TMChange}}%
20      \hbox to\z@{{\@nameuse{\psTshadowcolor}\copy\pst@hbox\hss}}}%
21      \pst@Verb{\tx@TMRestore}%

```

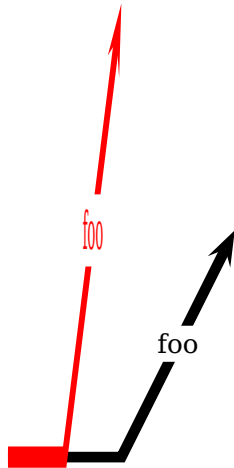
```

22 \box\pst@hbox}%
23 \endgroup}

```

## 7 Affin Transformations

```
\psAffinTransform [Options] {transformation matrix}{object}
```



```

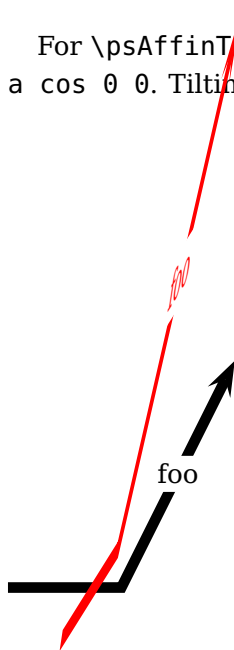
1 \pspicture(3,6)\psset{linewidth=4pt,arrows=->}
2 \psline(0,0)(1.5,0)(3,3)\rput*(2.25,1.5){foo}
3 \psAffinTransform{0.5 0 0 2 0 0}{\color{red}%
4 \psline[linecolor=red](0,0)(1.5,0)(3,3)\rput*(2.25,1.5){foo
5 \endpspicture

```

The transformation matrix must be a list of 6 values divided by a space. For a translation modify the last two values of  $1001dx dy$ . The values for  $dx$  and  $dy$  must be of the unit pt! For a rotation we have the transformation matrix

$$\begin{bmatrix} \cos(\alpha) & \sin(\alpha) & 0 \\ -\sin(\alpha) & \cos(\alpha) & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad (1)$$

For `\psAffinTransform` the four values have to be modified as  $\cos$   $\sin$   $-\sin$   $\cos$   $0$   $0$ . Tilting can be done with  $sx00sy00$ . All effects can be combined.



```

1 \pspicture(3,6)\psset{linewidth=4pt,arrows=->}
2 \psline(0,0)(1.5,0)(3,3)\rput*(2.25,1.5){foo}
3 \psAffinTransform{0.5 0.8 0.3 2 20 -20}{\color{red}%
4 \psline[linecolor=red](0,0)(1.5,0)(3,3)\rput*(2.25,1.5){foo
5 \endpspicture

```

## 8 List of all optional arguments for pst-3d

Key	Type	Default
viewpoint	ordinary	1 -1 1
viewangle	ordinary	0
normal	ordinary	0 0 1
embedangle	ordinary	0
Tshadowsize	ordinary	1
Tshadowangle	ordinary	60
Tshadowcolor	ordinary	lightgray

## References

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